

simple harmonic motion, problem set #2

1) Consider a horizontal tray with mass M which is attached to an ideal vertical spring with stiffness k . There is a brick with mass m sitting on this tray. See fig. 1. We push down the tray to $y = -A$, where $y = 0$ is the equilibrium point. We release the tray with zero velocity, $v = 0$. In other words $y(0) = -A$ and $v(0) = 0$ are the initial conditions. If A is large enough the brick will leave the tray.

- a) What is the angular frequency ω when brick is on the tray?
- b) Write down $y(t)$, assuming brick is on the tray.
- c) Now write down $a(t)$, the acceleration of the system.
- d) Draw the free body diagram for the brick. We call the normal force N .
- e) Write down the equation of motion for the brick and find $N(t)$, normal force as a function of time.
- f) What is the condition on N when brick leaves the tray?
- g) Find minimum A so that above condition has a solution, i.e. brick leaves the tray at some point. Find when and where the brick leaves the tray.

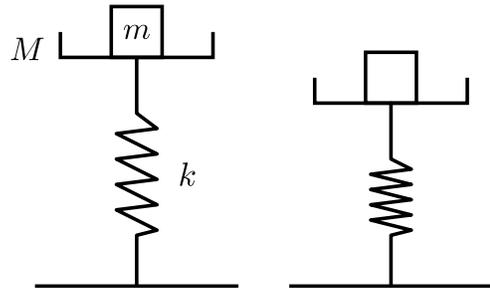


Figure 1: left: equilibrium, right: initial condition

2) A mass M is attached to a horizontal spring with stiffness k as shown in fig. 2. A block with mass m is sitting on top of it and there is friction between two masses. Take μ_S to be static friction coefficient. We pull the system of masses to point $x = A$ and release it; in other words initial conditions are $x(0) = A$ and $v(0) = 0$. If the amplitude A is large enough the block on top will slide. In all parts we are discussing the time before the block slides, if it does.

- a) What is the angular frequency ω ?
- b) Write down $x(t)$.
- c) Write down $a(t)$, the acceleration of the system.
- d) Draw the free body diagram for the block on top.
- e) Write down the equation of motion for the block on top and find $f_S(t)$, static friction force as a function of time.
- f) What is the condition so that the block on top slides at some point in time? Find when and where it happens.



Figure 2: If the amplitude is large enough the block on top will slide.