

tutorial #3 [electric circuits] .quiz

1) Alessandro Volta connects his car's $E = 12\text{ V}$ battery to two same parallel $R = 2\ \Omega$ coils immersed in the water. The wires that he connects the battery has $r = 0.5\ \Omega$ resistance. He wants to make some tea so he need $m = 0.3\text{ kg}$ water. The water is initially in temperature $T_i = 20^\circ$.

- Find the equivalence resistance of the whole circuit, r in series with two parallel R 's.
- Find the current passing through the battery.
- Find the power being supplied by the battery.
- The equivalence of two parallel R 's is $R/2$. Calculate the power that is delivered to the coils.
- Find the amount of energy needed to get water to boiling point.
- Using last two parts, how long it takes to boil the water?

a) from battery's point of view

$$R_{\text{eq}} = r + R/2 = 1.5\ \Omega$$

b) $V = R_{\text{eq}} I \Rightarrow I = \frac{12\text{V}}{1.5\ \Omega} = 8\text{ A}$

c) $P_{\text{tot}} = VI = 12\text{V} \times 8\text{ A} = 96\text{ W}$

d) We know the current passing through

$$\frac{R}{2}, \text{ the same } I = 8\text{ A}.$$

$$\text{so } P = \frac{R}{2} I^2 = 1.0\ \Omega \cdot 64\text{ A}^2 = 64\text{ W} \checkmark$$

or the voltage across $\frac{R}{2}$ is $\frac{R}{2} I = 8\text{ V} < 12\text{ V}$

$$\text{so } P = \frac{(8\text{V})^2}{1.0\ \Omega} = 64\text{ W} \checkmark$$

e) energy = $m c \Delta T = (0.3\text{ kg})(4200\text{ J/kg}^\circ\text{C})(100^\circ\text{C} - 20^\circ\text{C}) = 1.0 \times 10^5\text{ J}$

f) $\Delta t = \frac{\text{energy}}{P} = \frac{1.0 \times 10^5\text{ J}}{64\text{ W}} = 1.6 \times 10^3\text{ sec} \sim 27\text{ min.}$

